# Theoretical Study of the Conformational Isomerism of 2,4,6-Substituted 1,3,5-Trimethoxycalix[6]arenes 

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#### Abstract

For 2,4,6-trisubstituted 1,3,5-trimethoxycalix[6] arenes 1, two competing interconversion pathways have been postulated in the literature for the Cone/1,2,3Alternate exchange, viz the "tert-butyl through the annulus" and "lower rim through the annulus" pathways. Both pathways were compared with molecular modeling with the conjugate peak refinement method. One variable-size atom ( Sx ) was introduced to represent the lowerrim substituents R , abstracting the " $\mathrm{O}-\mathrm{CH}_{2}-$ rigid group" motifs to one " $\mathrm{O}-\mathrm{CH}_{2}-\mathrm{Sx}$ " group. Both the postulated mechanisms of Cone $\rightarrow 1,2,3$ Alternate isomerization are plausible. For large lower-rim substituents ( $\mathrm{Sx} \geq \approx 6 \AA$ ), the "tert-butyl through the annulus" mechanism is preferred over the "Sx through the annulus" mechanism. The calculated upper free energy barrier for the isomerization process is $17.5 \mathrm{kcal} \mathrm{mol}^{-1}$, reasonably close to the experimental value of approximately $21 \mathrm{kcal} \mathrm{mol}^{-1}$ (van Duynhoven et al. J. Am. Chem. Soc. 1994, 116, 5814).


## Introduction

Calix[4]arenes have proven to be useful building blocks in supramolecular chemistry, because of the possibility of selective functionalization and control over the conformation. ${ }^{1}$ The selective functionalization of calix[6]arenes has recently been explored, ${ }^{2}$ but in contrast to calix[4]arenes, it is difficult to immobilize the conformations of calix[6]arenes. The introduction of large lower-rim substituents ${ }^{3-5}$ and various bridges ${ }^{6,7}$ and caps ${ }^{8,9}$ have yielded a small number of conformationally fixed calix[6]arenes. The difficulty in freezing the conformation of calix[6]arenes is illustrated by the 2,4,6-trisubstituted 1,3,5trimethoxycalix[6]arenes 1 (Chart 1). Compound 1c was presented as the first example of a calix[6]arene frozen in the Cone conformation, ${ }^{10}$ but later it was shown ${ }^{5,11}$ that all calix[6]arenes $\mathbf{1}$ exist as two slowly exchanging conformers. The major conformer is a $C_{3 v}$ Cone and the minor one is a $C_{s} 1,2,3-$ Alternate ( $1,2,3 \mathrm{Alt}$ ), as determined by 2D NMR in $\mathrm{CDCl}_{3}$ and $\mathrm{CD}_{2} \mathrm{Cl}_{2}$ (Figure 1). ${ }^{5}$ The stability of both conformations has been explained by self-inclusion of the methoxy moieties, which gives rise to attractive $\mathrm{CH} \cdots \mathrm{p}$ interactions. ${ }^{5}$ The free energy differences between the stable conformers $\left(\Delta G^{\circ}\right)$ and the free energy changes of conformational exchange of $\mathbf{1}\left(\Delta G^{\ddagger}\right)$ have been determined (Table 1). ${ }^{5}$

The upper limit of the activation free energy barrier of $\approx 21$ $\mathrm{kcal} \mathrm{mol}{ }^{-1}$ for large lower-rim substituents R has been explained by assuming that conformational interconversion can proceed via two different pathways, viz., the " $p$-tert-butyl through the annulus" and the "lower rim through the annulus" mechanisms. ${ }^{5,11}$ For small R, the R group passes more easily through the annulus than the upper rim tert-butyl moiety. For large R, the passage of the R group is blocked and the tert-butyl substituent moves through the annulus. The latter process accounts for the maximum free energy barrier observed for large R. Contrary to the calix[4]arenes, the size of the calix[6]arene cavity is apparently large enough to allow the upper rim to move through the annulus, even when substituted with tert-butyl groups.

## CHART 1



| R | R |  |
| :--- | :--- | :--- |
| 1a $\mathrm{CH}_{2} \mathrm{C}(\mathrm{O}) \mathrm{NEt}_{2}$ | 1f | $\mathrm{CH}_{2}-\left(3-\mathrm{NO}_{2}-\mathrm{C}_{6} \mathrm{H}_{4}\right)$ |
| 1b $\mathrm{CH}_{2}-\mathrm{C}_{6} \mathrm{H}_{5}$ | 1g $\mathrm{CH}_{2}-\left(3-\mathrm{CN}_{5}-\mathrm{C}_{6}-\mathrm{H}_{5}\right)$ |  |
| 1c $\mathrm{CH}_{2} \mathrm{C}(\mathrm{O}) \mathrm{O}-t-\mathrm{Bu}$ | 1h | $\mathrm{CH}_{2}-(2-$ naphtyl) |
| 1d $\mathrm{CH}_{2}-\left(4-\mathrm{Br}_{5}-\mathrm{C}_{6} \mathrm{H}_{5}\right)$ | 1i | $\mathrm{CH}_{2}-\left(4-\mathrm{C}_{6} \mathrm{H}_{5}-\mathrm{C}_{6} \mathrm{H}_{4}\right)$ |
| 1e $\mathrm{PO}(\mathrm{OEt})_{2}$ |  |  |

The "upper rim through the annulus" mechanism has been postulated in order to explain the plateau of activation free energy reached with increasingly larger substituents R. ${ }^{5,11}$ In this paper, the conformational interconversions of calix[6]arenes $\mathbf{1}$ are investigated with molecular modeling to test the postulated isomerization mechanisms. All calix[6]arenes 1 in Table 1 (except 1e) contain a " $\mathrm{O}-\mathrm{CH}_{2}-$ rigid group" motif. A variablesize atom $\mathrm{Sx}(\mathrm{S} 1-\mathrm{S} 10)$ is introduced to represent the substituents R , reducing the " $\mathrm{O}-\mathrm{CH}_{2}-$ rigid group" motifs to one " $\mathrm{O}-$ $\mathrm{CH}_{2}-\mathrm{Sx}$ " group. In this way the large number of degrees of freedom is reduced somewhat. The two possible Cone/1,2,3Alt isomerization pathways were compared for different sizes of Sx. It will be shown that the "upper rim through the annulus" mechanism is indeed plausible and that the observed maximum


Figure 1. Major conformer Cone (lower) and minor conformer 1,2,3Alt (upper) of 1 (hydrogen atoms not shown).

TABLE 1: Thermodynamic and Kinetic Parameters ${ }^{5}$ for the Interconversion of Cone to $\mathbf{1 , 2 , 3 A l t}$ of Calix[6]arenes 1 in $\mathrm{CDCl}_{3}{ }^{a}$

| compound | $\Delta G^{\circ}$ | $\Delta G^{\ddagger}$ | compound | $\Delta G^{\circ}$ | $\Delta G^{\ddagger}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1 a}$ | 1.7 | 20.8 | $\mathbf{1 f}$ | 0.5 | 19.1 |
| $\mathbf{1 b}$ | 0.7 | 16.7 | $\mathbf{1 g}$ | 0.7 | 19.6 |
| $\mathbf{1 c}$ | 1.4 | 18.7 | $\mathbf{1 h}$ | 0.7 | 20.3 |
| $\mathbf{1 d}$ | 0.5 | 20.6 | $\mathbf{1 i}$ | 0.7 | 21.1 |
| $\mathbf{1 e}$ | 1.0 | 19.1 |  |  |  |

${ }^{a} \Delta G^{\circ}$ was measured at $303 \mathrm{~K} ; \Delta G^{\ddagger}$, at 328 K . Both are given in kilocalories per mole.
free energy barrier for isomerism can be explained by the two competing interconversion pathways.

## Experimental Section

Energy Minimizations. The energies of all conformations were minimized by the conjugate gradient followed by the Newton-Raphson method until the RMS (root-mean-square) value of the energy gradient was less than $10^{-12} \mathrm{kcal} \mathrm{mol}^{-1}$ $\AA^{-1}$. For the evaluation of the energy and gradients, version 24 b 2 of the CHARMM ${ }^{12}$ force field was used. A dielectric constant $\epsilon=1$ was used with no cutoff for the nonbonded interactions. Energies and derivatives of $\mathbf{1}$ were evaluated with the parameters, partial charges, and energy function as used previously. ${ }^{13}$ Two new united atoms (CH2E and Sx) were introduced for describing the 2,4,6 lower-rim substituent R (Chart 2 and Tables 2 and 3). The Sx atoms have been assigned no charge; the CH 2 E atom bears the total charge of the $\mathrm{CH}_{3}$ atoms of an anisole ring. The Sx atoms have the same mass as a C atom. The parameter files of quanta ${ }^{14}$ were adapted in order to produce graphical output with the $\mathrm{S} 1-\mathrm{S} 10$ atoms. Initial conformations were built from the Cone and 1,2,3-Alternate as calculated in ref 5 . Saddle points were refined by minimizing the gradient of the energy until the RMS gradient was less than $10^{-12} \mathrm{kcal} \mathrm{mol}{ }^{-1} \AA^{-1}$. The $\sim_{\text {AAA }}$ and $\sim_{\text {BBB }}$ conformations were built by setting the $\mathrm{CA}-\mathrm{CA}-\mathrm{OE}-\mathrm{CH} 2 \mathrm{E}$ dihedral (Chart 2) to $90^{\circ}$ or $-90^{\circ}$, respectively.

Normal Mode Calculation. All $3 N$ (in which $N$ is the number of atoms) modes were calculated. Each energyminimized conformation was checked to be a true minimum by checking the absence of negative frequencies and the

## CHART 2. New Atom Types (CH2E and Sx) with Partial Charges for the Lower Rim 2,4,6-Substituents R of 1



TABLE 2: Additional van der Waals Parameters

| atom type | $E_{\min }\left(\mathrm{kcal} \mathrm{mol}^{-1}\right)$ | $R_{\min } / 2(\AA)$ | remarks |
| :--- | :---: | :---: | :--- |
| CH2E | -0.1142 | 2.235 | CH2E parm19 $^{a}$ |
| S1 | -0.1811 | 2.165 | CH3E parm1 $^{a}$ |
| S2 | -0.1811 | 2.3133 | interpolated S1-S10 |
| S3 | -0.1811 | 2.4617 | interpolated S1-S10 |
| S4 | -0.1811 | 2.6100 | interpolated S1-S10 |
| S5 | -0.1811 | 2.7583 | interpolated S1-S10 |
| S6 | -0.1811 | 2.9067 | interpolated S1-S10 |
| S7 | -0.1811 | 3.0550 | interpolated S1-S10 |
| S8 | -0.1811 | 3.2333 | interpolated S1-S10 |
| S9 | -0.1811 | 3.3517 | interpolated S1-S10 |
| S10 | -0.1811 | 3.500 | long axis biphenyl $\approx 7 \AA$ |

${ }^{a}$ Parm19 is an older parametrization of charmm containing united atom models.

TABLE 3: Additional Bonded Parameters

| bond $\quad K_{\mathrm{b}}(\mathrm{kc}$ | $K_{\mathrm{b}}\left(\mathrm{kcal} \mathrm{mol}{ }^{-1} \AA^{-2}\right)$ | $r_{0}(\AA)$ | remarks |
| :---: | :---: | :---: | :---: |
| CH2E-OE | 296.70 | 1.45 | $=\mathrm{CT}-\mathrm{OE}$ |
| CH2E-S1 | 229.63 | 1.54 | $=\mathrm{CH} 2 \mathrm{E}-\mathrm{CH} 3 \mathrm{E}$ parm19 ${ }^{\text {a }}$ |
| CH2E-S2 | 229.63 | 2.1467 | interpolated S1-S10 |
| CH2E-S3 | 229.63 | 2.7533 | interpolated S1-S10 |
| CH2E-S4 | 229.63 | 3.3600 | interpolated S1-S10 |
| CH2E-S5 | 229.63 | 3.9667 | interpolated S1-S10 |
| CH2E-S6 | 229.63 | 4.5733 | interpolated S1-S10 |
| CH2E-S7 | 229.63 | 5.1800 | interpolated S1-S10 |
| CH2E-S8 | 229.63 | 5.7867 | interpolated S1-S10 |
| CH2E-S9 | 229.63 | 6.3933 | interpolated S1-S10 |
| CH2E-S10 | 229.63 | 7.0000 | $r_{0}=R_{\text {min }} \mathrm{vdW}$ radius S 10 |
| angle $\quad K$ | $K_{\theta}\left(\mathrm{kcal} \mathrm{mol}{ }^{-1} \mathrm{rad}^{-2}\right) \quad \theta_{0}(\mathrm{deg})$ |  |  |
| $\mathrm{CA}-\mathrm{OE}-\mathrm{CH} 2 \mathrm{E}$ | $2 \mathrm{E} \quad 110.0$ |  | 109.7 = $\mathrm{CA}-\mathrm{OE}-\mathrm{CT}$ |
| $\mathrm{OE}-\mathrm{CH} 2 \mathrm{E}-\mathrm{Sx}$ | Sx 75.7 |  | $110.1=\mathrm{OH1}-\mathrm{CT}-\mathrm{CT}$ |
| dihedral angle | le $\quad K_{\phi}\left(\mathrm{kcal} \mathrm{mol}^{-1}\right) \phi(\mathrm{deg})[n]$ |  |  |
| $\mathrm{X}-\mathrm{OE}-\mathrm{CH} 2 \mathrm{E}-\mathrm{X}$ | -X 0.10 |  | $0[3]=\mathrm{HA}-\mathrm{CT}-\mathrm{OE}-\mathrm{CA}$ |
| $\mathrm{CH} 2 \mathrm{E}-\mathrm{OE}-\mathrm{CA}-\mathrm{CA}$ | CA-CA 1.40 | 180 | $0[2]=\mathrm{CA}-\mathrm{CA}-\mathrm{OE}-\mathrm{CT}$ |

${ }^{a}$ Parm19 is an older parametrization of charmm containing united atom models.
presence of six zero frequencies. The maximum deviation from zero was in the order of $\approx 0.2 \mathrm{~cm}^{-1}$. The classical $\left(\Delta A_{\mathrm{cl}}\right)$ and quantum mechanical ( $\Delta A_{\mathrm{QM}}$ ) vibrational free energies as well as the zero-point correction energy $\left(\Delta A_{0}\right)$ were calculated: ${ }^{15}$

$$
\begin{gather*}
\Delta A_{\mathrm{QM}}=k T \sum_{i=7}^{3 N} \ln \left(1-e^{-h v_{i} / k T}\right)  \tag{1}\\
\Delta A_{\mathrm{cl}}=k T \sum_{i=7}^{3 N} \ln \left(\frac{h v_{i}}{k T}\right)  \tag{2}\\
\Delta A_{0}=\sum_{i=7}^{3 N} \frac{h v_{i}}{2} \tag{3}
\end{gather*}
$$



Figure 2. Six possible pathways for the $000000 \rightarrow 111000$ interconversion. Bold arrows denote rotation of the Sx-bearing ring, which can proceed in two ways: Sx or $t$-Bu through the annulus. Other arrows denote rotation of methoxy-bearing rings.
in which $k$ is the Boltzmann constant, $T$ is the temperature in kelvins, $N$ is the number of atoms, $h$ is the constant of Planck, and $v_{i}$ is the frequency of the $i$ th mode.

Setup of Interconversion Pathways. The digits in the names of the conformations indicate which aromatic ring has been inverted. For instance: 000000 is a Cone, 111000 is a $1,2,-$ 3Alt, 111111 is an inverted Cone, etc. In the 1,2,3Alt, either two rings bearing methoxy moieties and one ring bearing an Sx substituent have rotated with respect to the 000000 Cone ( 111000,001110 , or 100011 ), or one ring bearing a methoxy and two rings bearing Sx substituents (000111, 110001, or 011100 ). ${ }^{16}$ The interconversion pathways of Cone $\rightarrow 1,2,3 \mathrm{Alt}$ of $\mathbf{1}$ can thus be divided in two groups of three equivalent paths. We assume that the rotation of a methoxy-bearing ring will not be rate-limiting when Sx is larger than methyl, and therefore we have calculated only the $000000 \rightarrow 111000$ pathway. In this pathway, two rings bearing a methoxy group have to rotate (rings 1 and 3), as well as one ring bearing Sx (ring 2). For the rotation of a methoxy-bearing ring, only the "methoxy through the annulus" path is considered. The Sx-bearing ring can rotate with either Sx or $t$-Bu through the annulus, so that a total of six pathways have been taken into account (Figure 2). To vary the start and final conformations of the reaction path calculations, the CH2E atoms of the 2,4,6-substituents are made pointing outward (indicated with $\sim$ AAA ) or inward (indicated with $\sim$ BBB) with respect to the annulus. This doubles the number of interconversion pathways, because all interconversion steps were calculated with both the $\sim_{\text {AAA }}$ and $\sim_{\text {BBB }}$ conformers. Combinations of inward and outward positions are also possible, but they were not considered in order to save computational efforts. The radius of Sx was varied in 10 steps from $4.33 \AA$ (S1: $\mathrm{CH}_{3}$ extended atom) to $7.0 \AA$ ( S 10 : $\approx$ largest $\mathrm{C}-\mathrm{C}$ distance in a biphenyl unit). For each size of Sx, the lowest free energy transition state was determined for Sx or $t$-Bu through the annulus pathways. A total of 200 interconversions have been calculated. Free energy barriers were calculated with respect to the global lowest free energy conformation for each Sx substituent.

Reaction Path Calculations. The conjugate peak refinement (CPR) algorithm ${ }^{17-19}$ searches for maxima along the adiabatic energy valley connecting two local minima on an adiabatic energy surface. These maxima are refined to saddle points and represent the transition states of the reaction pathway between the two minima. All the degrees of freedom of the molecule can contribute to the reaction path. There is no need at all to choose a reduced reaction coordinate such as a rotation around a certain bond. The algorithm has been integrated into CHARMM ${ }^{12,15}$ in the TRAVEL module. First, all the interconver-
sions with the smallest $S x$ (S1) were calculated. As an initial guess, three intermediates were provided in which the aromatic ring was rotated 45,90 , and $135^{\circ}$, respectively, around the axis connecting the C -atoms ortho to the lower rim substituent. In all intermediates, the three methoxy moieties were rotated out of the cavity to make way for the rotating aromatic ring. The output of these calculations was used as initial guess for the calculations with the smallest one but Sx (S2), etc. The CPR method at first interpolates linearly between the Cartesian coordinates of the reactant, the product, and the initial intermediates. In a number of cases, these interpolations result in a path with some nonphysical segments. In the case of $\mathbf{1}$, methyl groups often inverted like umbrellas during a storm. This problem was resolved by deleting all hydrogens in such a trajectory and rebuilding them from internal coordinates, followed by further refinement of the trajectory by CPR. Only the highest saddle point in each trajectory was fully refined to save computational efforts.

## Results and Discussion

Energy Minimizations. All free energies in this paper were calculated including the quantum mechanical or the classical vibrational contributions. Since the differences between these contributions were small and in no case influenced the relative order of minimized conformers (or transition states), only free energies including the quantum mechanical contributions are discussed. Selected results of energy minimizations and normal mode calculations are presented in Table 4. Intermediate conformations of the $000000 \rightarrow 111000$ pathway (Figure 2) were also minimized but are not shown, since our primary interest was in the transition states connecting 000000 with 111000 , not in the conformational distribution of calix[6]arene 1. For all sizes of $S x$, the $111000 \sim$ ABB was the lowest potential energy conformer. However, when the vibrational free energy was taken into account, the $000000 \sim$ AAA was the most favorable conformer (Figure 4). This is in agreement with previous experimental findings ${ }^{5}$ that the Cone is the major conformer and the $1,2,3$ Alt is the minor (Table 1). In the Cone conformation the three OMe groups are filling the cavity, which is consistent with experimental data. ${ }^{5}$ This stabilization of the Cone will be the result of favorable van der Waals and/or electrostatic interactions, without the need of introducing "magic" forces (vide infra). The free energy of the Cone as a function of the radius of the $S x$ group was not constant but varied (Figure 3).

The maximum difference is $3.4 \mathrm{kcal} \mathrm{mol}^{-1}$ between calix[6]arene 1 with S3 substituents ( $0.5 \mathrm{kcal} \mathrm{mol}^{-1}$ ) and with S10 substituents ( $-2.9 \mathrm{kcal} \mathrm{mol}^{-1}$ ). An explanation for the maximum free energy for S 3 substituents can be found in Figure 4, where all of the calix[6]arene but the Sx atoms are overlapping. The Cone of calix[6]arene $\mathbf{1}$ having S3 substituents is the only conformer in Figure 4 having all three $\mathrm{C}_{\text {aro }}-\mathrm{O}-\mathrm{CH} 2 \mathrm{E}-\mathrm{S} 3$ dihedral angles (Chart 2) deviate from the optimal $180^{\circ}$.

Isomerizations. The free energies of the rate-limiting transition states of both isomerization mechanisms are presented in Table 5 and Figure 3. The free energy barrier for the " $t$ - Bu through the annulus" mechanism is reasonably constant, with a minimum of $15.7 \mathrm{kcal} \mathrm{mol}^{-1}$ for S 10 and a maximum of 17.8 $\mathrm{kcal} \mathrm{mol}{ }^{-1}$ for $\mathrm{S} 3-\mathrm{S} 5$. This isomerization barrier was expected to be nearly constant, since the tert-butyl moiety that passes through the annulus is in all cases the same. There was not much free energy difference when using either of the $\sim_{\text {AAA }}$ and $\sim_{\text {BBB }}$ start and final conformations. The calculated isomerization barriers indicate that the postulated " $t$-Bu through

TABLE 4: Normalized Results of Energy Minimizations and Vibrational Free Energy Calculations ${ }^{a}$ of Selected Conformers of 1 at $T=300 \mathrm{~K}$

| conformation | Sx | $\begin{aligned} & R_{\min } \\ & (\mathrm{A}) \end{aligned}$ | $n$ | $E_{\text {min }}$ | $\Delta A_{\text {qm }}$ | $\Delta A_{\text {cl }}$ | $\Delta A_{0}$ | $\Delta A_{\text {total }}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  | QM | cl |
| $000000 \sim$ AAA | S1 | 4.33 | 2 | 4.1 | -4.3 | -5.3 | -1.4 | 0.5 | 0.6 |
| $00000 \sim$ BBE | S1 | 4.33 | 2 | 3.0 | -3.9 | -4.8 | -1. | 0.0 | 0.0 |
| $111000 \sim$ B | S1 | 4.33 | 6 | 0.9 | -1.6 | -1.9 | -0. | 0.3 | 0.1 |
| $1000 \sim$ | S1 | 4.33 | 6 | 0.0 | 0.0 | 0.0 | 0.0 | 1.4 | . 1 |
| $000000 \sim$ AAA | S2 | 4.63 | 2 | 4.4 | -5.9 | -7.2 | 7 | -1.2 | -1.0 |
| $000000 \sim$ ввв | S2 | 4.63 | 2 | 3.3 | -4.5 | 5 | -1.4 | -0.5 | -0.4 |
| 000 | S2 | 4.63 | 6 | 1.2 | -1.7 | 2.2 | -0.8 | 0.1 | 0.1 |
| $1000 \sim$ | S2 | 4.63 | 6 | 0.4 | -0.1 | -0.4 | -0.4 | 1.3 | . 2 |
| $000000 \sim$ AAA | S3 | 4.92 | 2 | 4.6 | -4.5 | -5.8 | -1.8 | . 5 | 0.7 |
| 0000~ | S3 | 4.92 | 2 | 3.5 | -3.3 | -4.4 | -1.5 | . 8 | . 0 |
| $1000 \sim$ baA | S3 | 4.92 | 6 | 1.5 | -2.0 | -2.7 | -1.0 | 0.0 | 0 |
| $1000 \sim$ ABB | S3 | 4.92 | 6 | 0.9 | -0.6 | -1.0 | -0.6 | 1.2 |  |
| $\sim$ | S4 | 5.22 | 2 | 4.9 | -5.9 | -7.3 | 1.9 | -0.8 | -0.6 |
| 00~ | S4 | 5.22 | 2 | 3.6 | -3.4 | . 5 | - | . 7 | 0.8 |
| 1000~ | S4 | 5.22 | 6 | 1.7 | -2.2 | -3.0 | -1.1 | -0.2 | -0.1 |
| 1000~ | S4 | 5.22 | 6 | 1.3 | -1.0 | -1.5 | -0.7 | 1.0 | 0.9 |
| 000 | S5 | 5.52 | 2 | 5.6 | -8.1 | -9.8 | -2.3 | -2.6 | -2.4 |
| 00 | S5 | 5.52 | 2 | 3.7 | -4.8 | -6.0 | -1.7 | -0.6 | -0.5 |
| 1000 | S5 | 52 | 6 | 1.8 | -2.4 | -3.2 | -1.1 | -0.3 | 0.3 |
| 000 | S5 | 5.52 | 6 | 1.4 | -1.0 | -1. | -0.8 | 1.0 | 0.9 |
| 0000 | S6 | 5.81 | 2 | 5.9 | -8.0 | -9.8 | -2.3 | -2.4 | -2.1 |
| 000 | S6 | 5.81 | 2 | 3.4 | -4.5 | -5.8 | -1.7 | -0.7 | -0.6 |
| 1000 | S6 | 5.81 | 6 | 1.8 | -2.6 | -3.5 | -1.2 | -0.6 | -0.6 |
| 000 | S6 | 5.81 | 6 | 1.5 | -1.4 | -2.0 | -0.8 | 0.7 |  |
| 000~ | S7 | 6.11 | 2 | 6.0 | - | -10.0 | 4 | -2.4 | -2.2 |
| 000000~ | S7 | . 11 | 2 | 4.0 | -5.4 | -6.8 | -1.9 | -1.2 | -1.0 |
| $111000 \sim$ | S7 | 6.11 | 6 | 1.7 | -2.9 | -3.8 | -1.2 | -1.0 | -0.9 |
| $111000 \sim$ ABB | S7 | 6.11 | 6 | 1.6 | - | -2. |  | 0.4 |  |
| $000 \sim$ | S8 | 6.41 | 2 | 6.1 | -8.4 | -10.2 | -2.4 | -2.6 | $-2.2$ |
| 0000~ | S8 | 6.41 | 2 | 3.8 | -5.5 | -6.9 | -1.9 | -1.5 | -1.3 |
| $1000 \sim$ BAA | S8 | 6.41 | 6 | 2.9 | -4.4 | -5.5 | -1.4 | -1.5 | -1.5 |
| $111000 \sim$ | S8 | 6.41 | 6 | 2.8 | -3.3 | -4.1 | -1.1 | -0.1 | -0.2 |
| 0000 ~AAA | S9 | 6.70 | 2 | 6.2 | -8.6 | -10.4 | -2.4 | -2.7 | $-2.4$ |
| $000000 \sim$ ввв | S9 | 6.70 | 2 | 3.7 | -5.6 | -7.1 | -1.9 | -1.8 | -1.6 |
| $111000 \sim$ BAA | S9 | 6.70 | 6 | 3.0 | -4.6 | -5.7 | -1.5 | -1.6 | -1.5 |
| $111000 \sim$ ABB | S9 | 6.70 | 6 | 3.0 | -3.5 | -4.3 | -1.1 | -0.1 | -0.2 |
| $000000 \sim$ AAA | S10 | 7.00 | 2 | 6.3 | -8.8 | -10.7 | -2.5 | -2.9 | -2.6 |
| $000000 \sim$ ввв | S10 | 7.00 | 2 | 3.6 | -5.8 | -7.3 | -2.0 | -2.1 | -1.9 |
| $111000 \sim$ BAA | S10 | 7.00 | 6 | 3.2 | -4.9 | -6.0 | -1.5 | -1.8 | -1.7 |
| $111000 \sim$ ABB | S10 | 7. | 6 | 3.2 | -3.7 | -4.6 | -1.1 | -0.3 | -0.3 |

${ }^{a}$ Energies are given in kilocalories per mole.
the annulus" mechanism is indeed feasible. In all cases but one, the position of the rate-limiting step is the $100000 \rightarrow$ 110000 conversion. The exception is found for S10, where the rate-limiting step $101000 \rightarrow 111000$ is favored by only 0.2 kcal $\mathrm{mol}^{-1}$ over the $100000 \rightarrow 110000$ conversion. The free energy barriers for the $100000 \rightarrow 110000$ conversions are comparable (within $1.5 \mathrm{kcal} \mathrm{mol}^{-1}$ ) to the barriers of the $101000 \rightarrow 111000$ conversions, while the $000000 \rightarrow 100000$ steps have considerably higher free energy barriers ( $\approx 7 \mathrm{kcal} \mathrm{mol}{ }^{-1}$ higher). A "tertbutyl through the annulus" step is apparently sterically more hindered in the first step of the Cone $\rightarrow 1,2,3$ Alt isomerization than in either the second or third step (pathways 2 and 3 in Figure 2). The similarity of the rate-limiting " $t$-Bu through the annulus" transition states is clear in Figure 5, which shows that almost all variation is found in the positions of the Sx groups.

For the "Sx through the annulus" mechanism, the free energy of the saddle points is expected to increase for larger Sx. The increase will not be linear since the van der Waals interaction function, which dominates the transition-state energy for larger Sx, contains $1 / r^{6}$ and $1 / r^{12}$ terms and is therefore highly


Figure 3. Free energy (including quantum chemical vibrational contribution) as a function of the van der Waals radius $R_{\min }$ of the lower rim 2,4,6 substituents Sx . Solid diamonds indicate the free energy barriers of the "Sx through the annulus" pathway, and triangles indicate the "tert-butyl through the annulus" pathway. Open diamonds are the free energy barriers of true "Sx through the annulus" rotations (see text). Open squares indicate the free energy of the minimized $000000 \sim$ AAA conformers normalized to $R_{\min }=4.33 \AA$. Solid squares are the free energies of the $000000 \sim_{\text {AAA }}$ conformers, each normalized to $\Delta A_{\text {total }}=0 \mathrm{kcal} \mathrm{mol}^{-1}$, which were used as reference states for the free energy barriers of all isomerizations.


Figure 4. Energy-minimized $111000 \sim$ BAA (upper) and $000000 \sim$ AAA (lower) conformations with lower rim substituents S1-S10. Hydrogen atoms are not shown for clarity.
nonlinear. The lower rim substituent has three rotatable bonds, while the tert-butyl moiety has essentially only the phenylbutyl bond (not counting rotations around the $\mathrm{C}-\mathrm{Me}$ bonds). The conformational freedom of the Sx group is therefore larger, and the variation in the saddle point energies is expected to vary more than is the case with the tert-butyl moving through the annulus. This variation is indeed found. For instance, the differences between the calculated barriers starting from the $\sim_{\text {AAA }}$ of $\sim_{\text {BBB }}$ Cone conformers were larger than was the case for the "tert-butyl through the annulus" mechanism. For $\mathrm{Sx} \leq$ S3, the free energy barriers are comparable to the barriers of the "methoxy through the annulus" mechanism. In fact, the rate-limiting barriers for S 1 and S2 are rotations of methoxy moieties between inside and outside positions. The initial guesses for the travel calculations with S1 had their methoxy

TABLE 5: Free Energy Barriers of Both Isomerism Pathways of 1 as a Function of the Radius of the Lower Rim Substituent $\mathbf{S x}^{a}$

| Sx | $R_{\text {min }}(\AA)$ | $\Delta A^{\ddagger}(\mathrm{OSx})$ | path $($ step $)$ | $\Delta A^{\ddagger}(t-\mathrm{Bu})$ | path $($ step $)$ |
| :--- | :---: | :---: | :---: | :---: | :--- |
| S1 | 4.33 | $\mathbf{1 3 . 6}$ | $3(3) \sim$ BBB | 17.5 | $2(2) \sim$ BBB |
| S2 | 4.63 | $\mathbf{1 3 . 3}$ | $3(3) \sim$ BBB | 17.6 | $2(2) \sim_{\text {BBB }}$ |
| S3 | 4.92 | $\mathbf{1 1 . 8}$ | $2(1) \sim$ BBB | 17.8 | $2(2) \sim_{\text {BBB }}$ |
| S4 | 5.22 | $\mathbf{1 5 . 7}$ | $3(3) \sim_{\text {AAA }}$ | 17.8 | $2(2) \sim_{\text {BBB }}$ |
| S5 | 5.52 | $\mathbf{1 6 . 5}$ | $2(2) \sim$ AAA | 17.8 | $2(2) \sim_{\text {BBB }}$ |
| S6 | 5.81 | $\mathbf{1 7 . 5}$ | $3(3) \sim$ AAA | $\mathbf{1 7 . 6}$ | $2(2) \sim_{\text {AAA }}$ |
| S7 | 6.11 | 19.6 | $3(3) \sim$ AAA | $\mathbf{1 6 . 7}$ | $2(2) \sim_{\text {BBB }}$ |
| S8 | 6.41 | 22.1 | $1(1) \sim$ AAA | $\mathbf{1 6 . 5}$ | $2(2) \sim_{\text {BBB }}$ |
| S9 | 6.70 | 34.0 | $1(1) \sim$ AAA | $\mathbf{1 6 . 0}$ | $2(2) \sim_{\text {AAA }}$ |
| S10 | 7.00 | 49.4 | $1(1) \sim$ AAA | $\mathbf{1 5 . 7}$ | $3(3) \sim_{\text {AAA }}$ |

${ }^{a} \Delta A^{\ddagger}(\mathrm{OSx})$ and $\Delta A^{\ddagger}(\mathrm{t}-\mathrm{Bu})$ are free energy barriers (including quantum mechanical vibrational contribution) in kilocalories per mole of the "Sx group through the annulus" and "tert-butyl through the annulus" mechanisms, respectively. path (step) denotes where the ratelimiting step can be found in Figure 2. The free energies shown in boldface type denote the preferred pathway of the two considered isomerization processes.


Figure 5. Transition-state conformations of the "tert-butyl through the annulus" mechanism with lower rim substituents S1-S5 and S7S8 (top), S6 and S9 (middle), and S10 (bottom). Hydrogen atoms are not shown for clarity.
groups rotated outside the annulus because this enlarges the free diameter of the annulus and lowers the energy barrier for the rotations of larger Sx. Since the output trajectories of the calculations with $S x$ were input for the calculations with $S x+$ 1, already for S1 the methoxy groups had to rotate to outside positions. For S 3 , the rate-limiting interconversion is a "methoxy through the annulus" step. The dotted line in Figure 3 shows the free energy barrier of the "Sx through the annulus" mechanism calculated when only the rotations of the Sx-bearing rings were taken into account. For $S x \leq S 6$, the $S x$ group is still smaller than the diameter of the annulus. In Figure 6 the rate-limiting steps for $\mathrm{Sx}=\mathrm{S} 4-\mathrm{S} 6$ are shown. For these sizes of Sx , the Sx group of the rotating ring either has already passed


Figure 6. Transition-state conformations with lower rim substituents S4 (top) to S6 (bottom) of the "Sx through the annulus" mechanism. Hydrogen atoms are not shown for clarity.
or still has to pass the smallest diameter of the annulus. The passage of the $S x$ group through the annulus is not rate-limiting, but the rearrangements to put the Sx group in the center of the annulus before or after the passage. Only when $\mathrm{Sx}>\mathrm{S} 6$ the passage of the $S x$ group through the annulus becomes ratelimiting, as can be seen in Figure 6. The Sx group is located at the smallest diameter of the annulus, as expected if the steric hindering of the passage of this group is rate-limiting. The $\mathrm{C}_{\text {aro }}-\mathrm{O}-\mathrm{CH} 2 \mathrm{E}-\mathrm{Sx}$ dihedral angles (Chart 2) of the rotating ring are all $\approx 0^{\circ}$, allowing the Sx group to pass exactly through the center of the annulus. The calix[6]arenes $\mathbf{1}$ used in experiments (Table 1$)^{5}$ had a similar " $\mathrm{O}-\mathrm{CH}_{2}-$ rigid group" motif as the $\mathrm{O}-\mathrm{CH}_{2}-\mathrm{Sx}$ used in the calculations. Therefore, we predict that the "Sx through the annulus" interconversions
of calix[6]arenes $\mathbf{1}$ proceed via a similar folding, which allows the rigid substituent to pass through the center of the annulus. We also predict that without the $\mathrm{CH}_{2}$ spacer, the ability will be reduced of positioning the Sx group at the center of the annulus, and the isomerization barrier will be increased.

The Preferred Pathway. For $S x=S 6(5.81 \AA)$, the barriers of both isomerization mechanisms are equal within 0.1 kcal $\mathrm{mol}^{-1}$. The calculated free energy barriers for the "tert-butyl through the annulus" mechanism show a standard deviation of $0.8 \mathrm{kcal} \mathrm{mol}^{-1}$. This free energy barrier is expected to be constant, so this number is used as an estimation of the variation in the calculated free energies. With this variation, the graphs of the "tert-butyl through the annulus" and "Sx through the annulus" intersect between S5 and S6. Because only for $S x \geq$ S7 does the passage of the Sx group through the annulus become rate-limiting in the "Sx through the annulus" pathway, we conclude that the "tert-butyl through the annulus" becomes preferred for $S x \geq S 7(6.11 \AA)$. The calculated free energy limit for the Cone $\rightarrow 1,2,3$ Alt interconversion barrier is 17.5 $\mathrm{kcal} \mathrm{mol}{ }^{-1}$. This number is reasonably close to the experimental $21 \mathrm{kcal} \mathrm{mol}^{-1}$, given the crude model of one uncharged atom of variable size as model for a range of lower-rim substituents and the neglect of solvent effects. However, we do not expect significant solvent effects in chloroform because 1,3,5trimethoxycalix[6]arenes do not possess a real cavity that can be stabilized by solvent inclusion. In addition to this, a recent theoretical study on tetramethoxycalix[4]arene showed that dichloromethane is able to stabilize the cone with respect to the other conformations, but chloroform is not. ${ }^{20}$

## Conclusions

The present study shows that the postulated competing mechanisms of Cone $\rightarrow 1,2,3$ Alt isomerization, the "tert-butyl through the annulus" and "Sx through the annulus" pathways, are indeed plausible. For large lower-rim substituents ( $\mathrm{Sx} \geq$ $\approx 6 \AA$ ), the "tert-butyl through the annulus" mechanism is preferred over the "Sx through the annulus" mechanism. The calculated upper free energy barrier for the isomerization process is $17.5 \mathrm{kcal} \mathrm{mol}^{-1}$, reasonably close to the experimental value of approximately $21 \mathrm{kcal} \mathrm{mol}^{-1}$. The successful calculations on systems with many degrees of freedom is encouraging and can be useful to steer the future design of fixed conformations.

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